

## **Programme Name: MSc Mathematics**

### **Programme Outcomes**

The Program Objectives are the knowledge skills and attributes which the students have at the time of post-graduation. At the end of the program, the student will be able to:

- To provide comprehensive curriculum to groom the students into qualitative scientific man power .
- Enable students to enhance mathematical skills and understand the fundamental concepts of pure and applied mathematics.
- To provide qualitative education through effective teaching learning processes by introducing projects, participative learning and latest software tools.
- To inculcate innovative skills, team work, ethical practices among students so as to meet societal expectations.
- To encourage collaborative learning and application of mathematics to real life situations.
- To inculcate the curiosity for mathematics in students and to prepare them for future.

### **Programme Specific Outcomes**

- Understanding of the fundamental axioms in mathematics and capability of developing ideas based on them.
- Inculcate mathematical reasoning.
- Prepare and motivate students for research studies in mathematics and related fields.
- Provide knowledge of a wide range of mathematical techniques and application of mathematical methods/tools in other scientific and engineering domains.
- Provide advanced knowledge on topics in pure mathematics, empowering the students to pursue higher degrees at reputed academic institutions.
- Strong foundation on algebraic topology and representation theory which have strong links and application in theoretical physics, in particular string theory.
- Good understanding of number theory which can be used in modern online cryptographic technologies.
- Nurture problem solving skills, thinking, creativity through assignments, project work.
- Assist students in preparing (personal guidance, books) for competitive exams e.g. NET, GATE, etc.

## Course Outcomes

Semester-I		
Course Code	Course Name	Course Outcomes
MM 1.1	Real analysis	<p>Knowledge gained:</p> <ul style="list-style-type: none"> <li>• Basic definition of metric space, norm linear space and inner product space.</li> <li>• Series and sequence of continuous functions.</li> <li>• Equi continuous families, Arzela - Ascoli Theorem and Stone-Weierstras Theorem.</li> <li>• Function of several variables and differentiation in <math>R_n</math>.</li> <li>• Inverse and Implicit function theorem.</li> <li>• Sub manifolds of <math>R_n</math> and Rank theorem.</li> </ul> <p>Skills gained:</p> <ul style="list-style-type: none"> <li>• Continuous functions on <math>[0,1]</math> as a metric space.</li> <li>• The notion of convergence in <math>C[0,1]</math> as a metric space.</li> <li>• Differentiability of functions in several variables and their relation to partial derivatives.</li> <li>• Realizing the differentials in terms of geometric properties.</li> </ul> <p>Competency developed:</p> <ul style="list-style-type: none"> <li>• Ability to handle convergence of series and sequence of functions.</li> <li>• Ability to differentiate functions in <math>R_n</math>.</li> </ul> <p>Apply Implicit and inverse function theorem, moving towards calculation manifolds.</p>
MM 1.2	Algebra- I	<p>Knowledge gained:</p> <ul style="list-style-type: none"> <li>• Groups , dihedral groups, cyclic groups and their properties</li> <li>• Isomorphism, check digits sylow's theorem and their applications</li> <li>• Fields ring homeomorphisms</li> <li>• Eigen values, diagonalization of matrices and reduction of systems of linear equations into simpler systems of easily tractable nature.</li> <li>• Vector theory: subspace, basis, linear independence, inner product spaces etc.</li> <li>• Applications of matrix algebra.</li> <li>• Matrix manipulations.</li> <li>• Handing of systems of linear equations</li> </ul> <p>Skills gained:</p> <ul style="list-style-type: none"> <li>• Matrix manipulations.</li> <li>• Handing of systems of linear equations.</li> </ul>

		<ul style="list-style-type: none"> <li>• Use mathematical software to solve problems on linear systems.</li> <li>• Ability to go abstract from concrete: from concrete notion of solution spaces to vector spaces.</li> <li>• Linear modelling problems</li> </ul> <p>Competency developed:</p> <ul style="list-style-type: none"> <li>• Solving Systems of linear equations.</li> </ul> <p>Qualitative analysis of systems of linear equations</p>
<b>MM 1.3</b>	<b>Discrete Mathematics</b>	<p>Knowledge gained:</p> <ul style="list-style-type: none"> <li>• Basic statements and notations ,concepts of connectiveness</li> <li>• Basic combinatorics, induction, inclusion exclusion, pigeon hole principle.</li> <li>• More advance topics in combinatorics : recurrence relations, generating functions, counting principles, principle of inclusion and exclusion</li> <li>• Four color problems , multigraphs , eulerian ,Hamiltonian graphs</li> <li>• Application to real life problems such as network theory, data structure, optimization etc.</li> <li>• Monoids and groups ,coding, decoding and error correction</li> </ul> <p>Skills gained:</p> <ul style="list-style-type: none"> <li>• Efficiency in handling with discrete structures.</li> <li>• Efficiency in Set theory and handling formal of notions of size.</li> <li>• Efficiency in notions of matching, ordering, planarity.</li> <li>• Efficiency in solving concrete combinatorial problems whose presence is ubiquitous in science and engineering.</li> </ul> <p>Competency developed:</p> <ul style="list-style-type: none"> <li>• Ability to deal with notions of mapping and via that notion ability to tackle various notions of infinity like countable, uncountable etc.</li> <li>• Ability to use graphs as unifying theme for various combinatorial problems.</li> </ul>
<b>MM-1.4</b>	<b>Ordinary Differential Equations</b>	<p>Knowledge gained:</p> <ul style="list-style-type: none"> <li>• Differential equations , and their types</li> <li>• Fundamental concepts about their existence and uniqueness</li> <li>• Concepts and applications of eigen value problem</li> <li>• Sturm Liouville problem</li> <li>• Power series</li> <li>• Critical points and stability</li> </ul>

		<ul style="list-style-type: none"> <li>• non-linear autonomous system</li> </ul> <p>Skills gained:</p> <ul style="list-style-type: none"> <li>• Apply various power series methods to obtain series solutions of differential</li> <li>• Ability to Solve problems of ordinary differential equations arising in various fields.</li> <li>• Ability to stabilized the given equations</li> </ul> <p>Competency developed:</p> <ul style="list-style-type: none"> <li>• Apply various power series methods to obtain series solutions of differential</li> <li>• Ability to Solve problems of ordinary differential equations arising in various fields.</li> <li>• Ability to stabilized the given equations</li> </ul> <ul style="list-style-type: none"> <li>• Solving Systems of linear &amp; equations.</li> <li>• Qualitative analysis of systems of linear &amp; equations.</li> <li>• Ability to find critical points and phase plane</li> </ul>
MM-1.5	<b>Classical Mechanics</b>	<p>Knowledge gained:</p> <ul style="list-style-type: none"> <li>• the concept of functional and determine stationary paths of a functional to deduce the differential equation for stationary paths</li> <li>• Use Euler-Lagrange equation to find stationary paths and its applications in some classical fundamental problems</li> <li>• Define and understand basic mechanical concepts related to discrete and continuous mechanical systems.</li> <li>• describe and understand the motion of a mechanical system using Lagrange- Hamilton formalization.</li> </ul> <p>Skills gained:</p> <ul style="list-style-type: none"> <li>• Understand the concept of functional and determine stationary paths of a functional to deduce the differential equation for stationary paths.</li> <li>• Use Euler-Lagrange equation to find stationary paths and its applications in some classical fundamental.</li> <li>• describe and understand the motion of a mechanical system using Lagrange- Hamilton formalism..</li> </ul> <p>Competency developed:</p> <ul style="list-style-type: none"> <li>• Demonstrate good experimental practice, including accurate record keeping,</li> </ul>

		The planning and execution of experiments
<b>II Semester</b>		
<b>Course Code</b>	<b>Course Name</b>	<b>Course Outcomes</b>
<b>MM-2.1</b>	<b>Complex Analysis</b>	<p>Knowledge gained:</p> <ul style="list-style-type: none"> <li>• Introduce and develop a clear understanding of the fundamental concepts of Complex Analysis such as analytic functions, Cauchy- Riemann relations and harmonic functions</li> <li>• make students equipped with the understanding of the fundamental concepts of complex variable theory</li> <li>• enable students to acquire skill of contour integration to evaluate complicated real integrals via residue calculus</li> <li>• .</li> </ul> <p>Skills gained:</p> <ul style="list-style-type: none"> <li>• Know the fundamental concepts of complex analysis.</li> <li>• Evaluate complex integrals and apply Cauchy integral theorem and formula</li> <li>• Evaluate limits and checking the continuity of complex function &amp; apply the concept of analyticity and the Cauchy-Riemann equations.</li> </ul> <p>Competency developed:</p> <ul style="list-style-type: none"> <li>• Establish the capacity for mathematical reasoning through analysing, proving and explaining concepts from complex analysis</li> <li>• Extend their knowledge to pursue research in this field explaining concepts from complex analysis</li> </ul>
<b>MM 2.2</b>	<b>Algebra II</b>	<p>Knowledge gained:</p> <ul style="list-style-type: none"> <li>• Solving polynomial equations using formulas for roots</li> <li>• How to test if a polynomial is irreducible Finite Field</li> <li>• Understanding which equations can be solved using radicals</li> </ul> <p>Skills gained:</p> <ul style="list-style-type: none"> <li>• Ability to understand/obtain the roots of a polynomial equation if the same has (or can be reduced to) degree less than five.</li> <li>• Facility in working with finite fields</li> </ul>

		<ul style="list-style-type: none"> <li>Applying the concept of a field extension to various mathematical problems</li> </ul> <p>Competency developed:</p> <ul style="list-style-type: none"> <li>Facility in handling problems involving polynomial equations</li> <li>Applying mathematical methods to the real-life problems including cryptography.</li> <li>Highly developed reasoning ability</li> </ul>
<b>MM 2.3</b>	<b>Partial Differential Equations</b>	<p>Knowledge gained:</p> <ul style="list-style-type: none"> <li>first and higher order partial differential equations and their classification. This course explains various</li> <li>analytic methods for computing the solutions of various partial differential equations. It also first and higher</li> <li>wave equation of string, diffusion equations and heat flow equation to students</li> </ul> <p>Skills gained:</p> <ul style="list-style-type: none"> <li>Understand partial differential equations of first order (linear and nonlinear), second and higher order.</li> <li>Apply various analytic methods for computing solutions of various PDEs.</li> <li>Determine integral surfaces passing through a curve, characteristic curves of second order PDE and compatible systems</li> </ul> <p>Competency developed:</p> <ul style="list-style-type: none"> <li>Understand the formation and solution of some significant PDEs like wave equation, heat equation and diffusion equation.</li> </ul> <p>Apply the knowledge of PDEs and their solutions in order to understand physical phenomena.</p>
<b>MM 2.4</b>	<b>Topology</b>	<p>Knowledge gained:</p> <ul style="list-style-type: none"> <li>Topological Spaces and their importance</li> <li>Base and sub base of topology</li> <li>Compact space</li> <li>Equivalence of countability</li> <li>Lindelof property</li> </ul> <p>Skills gained</p> <ul style="list-style-type: none"> <li>the concepts of topological spaces and the basic definitions of open sets, neighbourhood, interior, exterior, closure and their axioms for defining topological space.</li> <li>the concept of Bases and Sub bases, create new topological spaces by using subspace.</li> <li>Understand continuity, compactness, connectedness</li> </ul>

		<p>homeomorphism and topological properties.</p> <p>Competency developed:</p> <ul style="list-style-type: none"> <li>Understand how points of space are separated by open sets, Housdroff spaces and their importance.</li> </ul> <p>Understand regular and normal spaces and some important theorems in these spaces</p>
<b>MM 2.5</b>	<b>Introduction to computers and C programming</b>	<p>Knowledge gained:</p> <ul style="list-style-type: none"> <li>concept of C fundamental</li> <li>concept of I/O operations</li> <li>concept of control statement</li> </ul> <p>Skills gained:</p> <ul style="list-style-type: none"> <li>c programming skills</li> <li>switch over to any language in future</li> <li>ability to work with arrays of complex objects</li> <li>understanding of code organization</li> </ul> <p>Competency developed:</p> <ul style="list-style-type: none"> <li>ability to handle possible errors during program execution</li> <li>able to develop applications in daily life</li> </ul>
<b>III Semester</b>		
<b>Course Code</b>	<b>Course Name</b>	<b>Course Outcomes</b>
<b>MM 3.1</b>	<b>Functional Analysis</b>	<p>Knowledge gained:</p> <ul style="list-style-type: none"> <li>Concept of normed linear spaces and inner product spaces.</li> <li>Concept of bounded linear operators between these spaces.</li> <li>Concept of the dual space of a normed linear space.</li> <li>Concept of compact, self-adjoint and normal operators.</li> </ul> <p>Concept</p> <p>Skills gained:</p> <ul style="list-style-type: none"> <li>Using topology to work with infinite dimensional vector spaces.</li> <li>Using careful analysis to show that certain spaces of functions are complete.</li> <li>Comparing the differences between finite and infinite dimensional spaces.</li> <li>Comparing the differences between Banach and Hilbert spaces.</li> <li>Analysing the structure of the spectrum of certain operators</li> </ul> <p>Competency developed:</p> <ul style="list-style-type: none"> <li>Working with a complete orthogonal set a.k.a. Schauder basis in a Hilbert space.</li> </ul>

		<ul style="list-style-type: none"> <li>Investigating the best approximation of a given vector by vectors in a given subspace.</li> <li>Computing the dual spaces of certain Banach spaces.</li> </ul> <p>Working with weak and weak* topologies on normed linear spaces</p>
<b>MM 3.2</b>	<b>Differential Geometry</b>	<p>Knowledge gained:</p> <ul style="list-style-type: none"> <li>basic concepts of differential geometry</li> <li>deal with geometry of curves and spaces using the methods of differential calculus</li> </ul> <p>Skills gained:</p> <ul style="list-style-type: none"> <li>Understand the basic concepts and results related to space curves, tangents, normal and surfaces.</li> <li>Explain the geometry of different types of curves and spaces.</li> <li>Explain the physical properties of different curves and spaces.</li> </ul> <p>Competency developed:</p> <ul style="list-style-type: none"> <li>Understand principal directions and curvatures, asymptotic lines and then apply their important theorems and results to study various properties of curves and surfaces</li> </ul>
<b>MM 3.3</b>	<b>Numerical Analysis I</b>	<p>Knowledge gained:</p> <ul style="list-style-type: none"> <li>The knowledge of Numerical Mathematics to solve problems efficiently arising in science, engineering and economics etc.</li> <li>Identify and analyze different types of errors encountered in numerical computing.</li> <li>Create, select and apply appropriate numerical techniques with the understanding of their limitations so that any possible modification in these techniques could be carried out in further research.</li> </ul> <p>Skills gained :</p> <ul style="list-style-type: none"> <li>Utilize the tools of the Numerical Mathematics in order to formulate the real-world problems from the view point of numerical mathematics.</li> <li>the basic concepts of Numerical Mathematics in order to solve the problems arising in various fields of application</li> <li>, analysis and application of different numerical methods to solve the problems, viz. system of linear &amp; nonlinear equations, numerical initial and boundary value problems of ordinary differential equations etc.</li> </ul> <p>Competency developed:</p> <ul style="list-style-type: none"> <li>Design, analyze and implement of numerical methods for solving different types of problems, viz.</li> <li>Identify the challenging problems in continuous mathematics (which are difficult to deal with analytically) and find their</li> </ul>

		appropriate solutions accurately and efficiently.
<b>MM 3.4</b>	<b>Fluid Mechanics I</b>	<p>Knowledge gained:</p> <ul style="list-style-type: none"> <li>• Understand the concept of rotational and ir-rotational flow, stream functions, velocity potential, sink, source, vortex etc.</li> <li>• analyze simple fluid flow problems (flow between parallel plates, flow through pipe etc.) with Navier- Stoke's equation of motion.</li> </ul> <p>Skills gained:</p> <ul style="list-style-type: none"> <li>• understand the phenomenon of flow separation and boundary layer theory</li> <li>• understand the concept of thermal conductivity.</li> </ul> <p>Competency developed:</p> <ul style="list-style-type: none"> <li>• learn about the fundamental equations of the flow and energy</li> </ul>
<b>MM 3.5</b>	<b>Graph Theory I</b>	<p>Knowledge gained:</p> <ul style="list-style-type: none"> <li>• Concept of fundamental circuits</li> <li>• Eulerian graph</li> <li>• Solve problems using basic graph theory</li> </ul> <p>Skills gained:</p> <ul style="list-style-type: none"> <li>• Identify induced sub graphs</li> <li>• Determine whether graphs are eulerian / Hamiltonian</li> <li>• Solve problems involving vertex connectivity and edge connectivity</li> </ul> <p>Competency developed:</p> <ul style="list-style-type: none"> <li>• Model real world problem using graph theory</li> </ul>
<b>IV Semester</b>		
<b>Course Code</b>	<b>Course Name</b>	<b>Course Outcomes</b>
<b>MM 4.1</b>	<b>Measure Theory</b>	<p>Knowledge gained:</p> <ul style="list-style-type: none"> <li>• Definition and properties of the exterior measure on <math>\mathbb{R}^d</math>.</li> <li>• Measurable sets and Lebesgue measure, construction of non-measurable sets.</li> <li>• Measurable functions.</li> <li>• Lebesgue integration, convergence theorems for Lebesgue integrals and Fubini's theorem.</li> <li>• <math>L^p</math> spaces and Fourier inversion formula</li> <li>• .Connection between differentiation and integration in the context of Lebesgue theory</li> </ul> <p>Skills gained:</p> <ul style="list-style-type: none"> <li>• Computation of Lebesgue measures.</li> <li>• Establishing measurability or non-measurability of sets and</li> </ul>

		<p>functions.</p> <ul style="list-style-type: none"> <li>• Approximating measurable functions by simple and step functions.</li> <li>• Computation of Lebesgue integrals, applications to volume calculations and Fourier analysis.</li> <li>• Deciding under which conditions the fundamental theorem of calculus is applicable in the context of Lebesgue integration</li> </ul> <p>Competency developed:</p> <ul style="list-style-type: none"> <li>• Understanding that Lebesgue integration can solve certain problems.</li> </ul>
<b>MM 4.2</b>	<b>Advanced Mathematical Methods</b>	<p>Knowledge gained:</p> <ul style="list-style-type: none"> <li>• Definition of tensor.</li> <li>• Application of laplace transform of PDE</li> <li>• First and second kind of fredholem volterra</li> <li>• Perturbation method</li> <li>• Concept of linear programming</li> <li>• Concept of duality</li> </ul> <p>Skills gained:</p> <ul style="list-style-type: none"> <li>• Computation of covariant and its derivatives.</li> <li>• Establishing linear integral equations.</li> <li>• Approximating measurable functions by simple and step functions.</li> <li>• Computation of asymptotic series .</li> </ul> <p>Competency developed:</p> <ul style="list-style-type: none"> <li>• Understanding graphical method and standard LLP and their solutions</li> </ul>
<b>MM 4.3</b>	<b>Numerical Analysis II</b>	<p>Knowledge gained:</p> <ul style="list-style-type: none"> <li>• Concept of single steps and multi steps method</li> <li>• Concept of hyperbolic, parabolic, elliptic</li> <li>• The differential equations and its solutions</li> </ul> <p>Skills developed:</p> <ul style="list-style-type: none"> <li>• Numerical methods for initial value problems for ODE and PDE</li> <li>• Practical solution of problems using C++</li> <li>• Exact , approximate , and numerical methods to solve to solve the resulting equations</li> <li>• System of linear equation by direct method</li> </ul> <p>Competency developed:</p> <ul style="list-style-type: none"> <li>• Simpler methods</li> <li>• Ability to use iterative methods to solve system of non linear equations</li> </ul>

<b>MM 4.4</b>	<b>Graph Theory II</b>	<p>Knowledge gained:</p> <ul style="list-style-type: none"> <li>• Concept of geometric dual of the graph</li> <li>• Concept of combinatorial of the graph</li> <li>• Concept of planar graph</li> <li>• Concept of colouring, covering</li> <li>• Concept of factorization</li> </ul> <p>Skills gained</p> <ul style="list-style-type: none"> <li>• Able to color the graph</li> <li>• Able to define four color problem</li> <li>• Ability to represent the graph in a computer</li> </ul> <p>Competency developed:</p> <ul style="list-style-type: none"> <li>• Model real world problem using graph theory</li> </ul>
<b>EI 4.5</b>	<b>Fluid Mechanics II</b>	<p>Knowledge gained:</p> <ul style="list-style-type: none"> <li>• Understand the basic principles of fluid mechanics, such as Lagrangian and Eulerian approach, conservation of mass etc.</li> <li>• Stress and strain components</li> <li>• Concept of pi theorem with its application</li> </ul> <p>Skills gained</p> <ul style="list-style-type: none"> <li>• Use thermal conductivity of flow</li> <li>• The concept of rotational and ir rotational flow, stream functions, velocity potential, sink, source, vortex etc.</li> <li>• Analyse simple fluid flow problems (flow between parallel plates, flow through pipe etc.) with Navier - Stoke's equation of motion.</li> </ul> <p>Competency developed:</p> <ul style="list-style-type: none"> <li>• the phenomenon of flow separation and boundary layer theory.</li> </ul>